



DANISH RESEARCH
CENTRE FOR
MAGNETIC RESONANCE

DTU DTU
 Health Tech



Hvidovre
Hospital

Field calculations with SimNIBS

Axel Thielscher
Guilherme B. Saturnino

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Overview

Terminology:

- Electric field & current density
- Field strength, normal component: What are they, and which should we report?
- from TDCS to TACS (and TRNS)

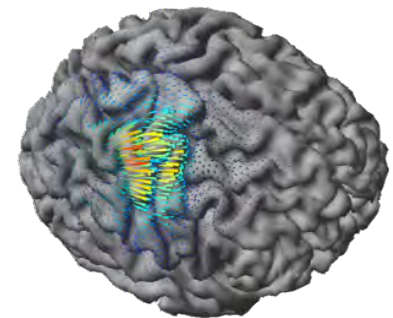
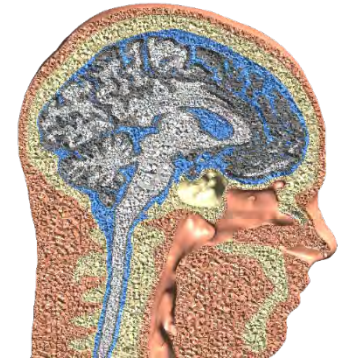
Segmentation accuracy and fields

- MR images to get robust segmentations

SimNIBS Workflow

Upcoming features: TES optimization, TMS optimization

Practical Exercise: Overview



Electric field and current density

Ohm's law $\vec{j} = \sigma \vec{E}$

\vec{j} current density in **A/m²**

how much current flow per area unit

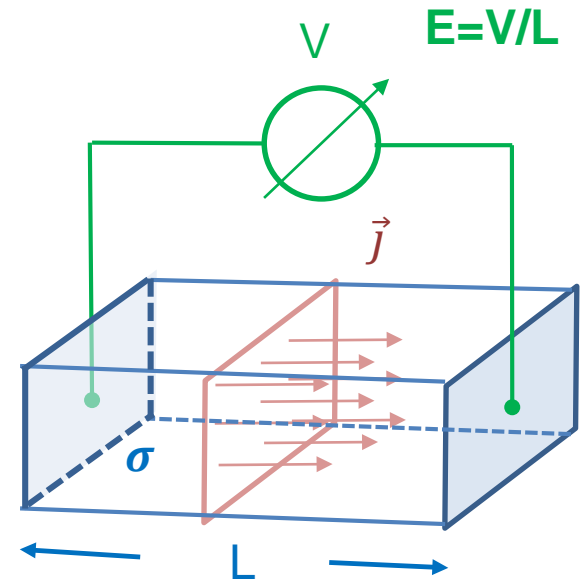
\vec{E} electric field in **V/m**

which potential (i.e. energy) difference per length unit

σ conductivity in **S/m**

fundamental property of a material that quantifies how well it conducts electric current

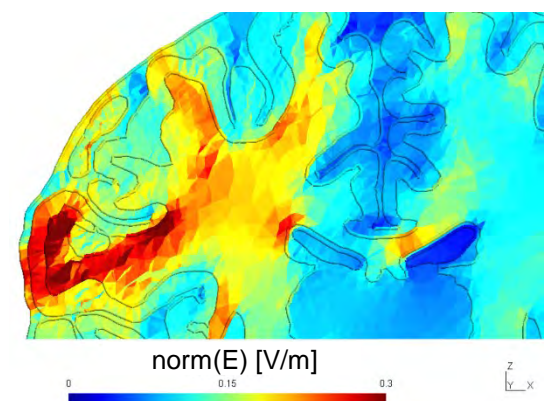
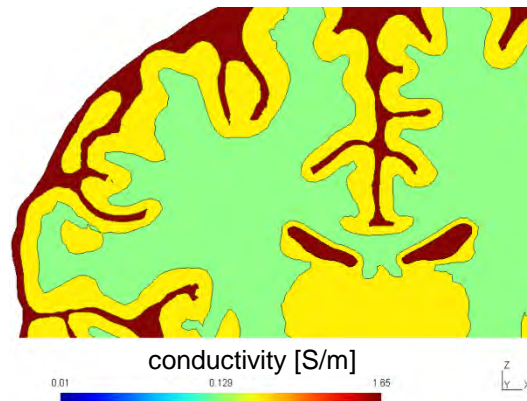
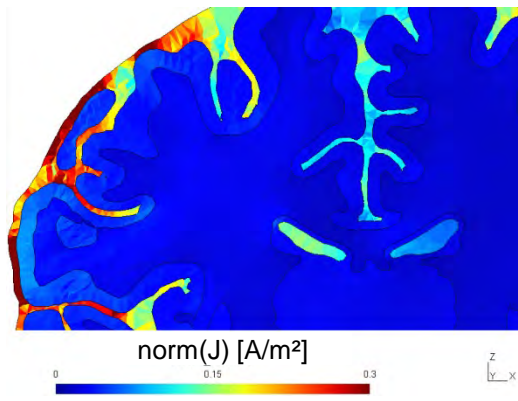
σ is the inverse of the resistivity ρ : $\sigma=1/\rho$
 ρ is in $\Omega \cdot \text{m}$



Example: Current flow from left to right in homogeneous conductor

Electric field and current density

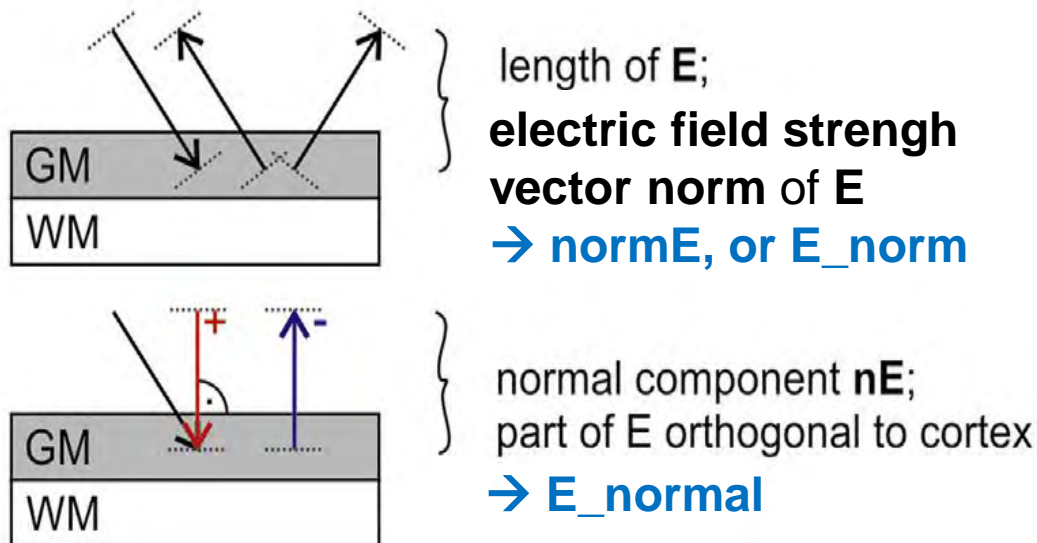
$$\vec{J} = \sigma \cdot \vec{E}$$



1 mA “standard” M1 montage, coronal cut at the level of M1, only CSF, GM and WM

- J and E are interchangeable.
- We usually report E, because nerve membrane polarization is dependent on E (or its spatial derivative)

Electric field strength vs normal component

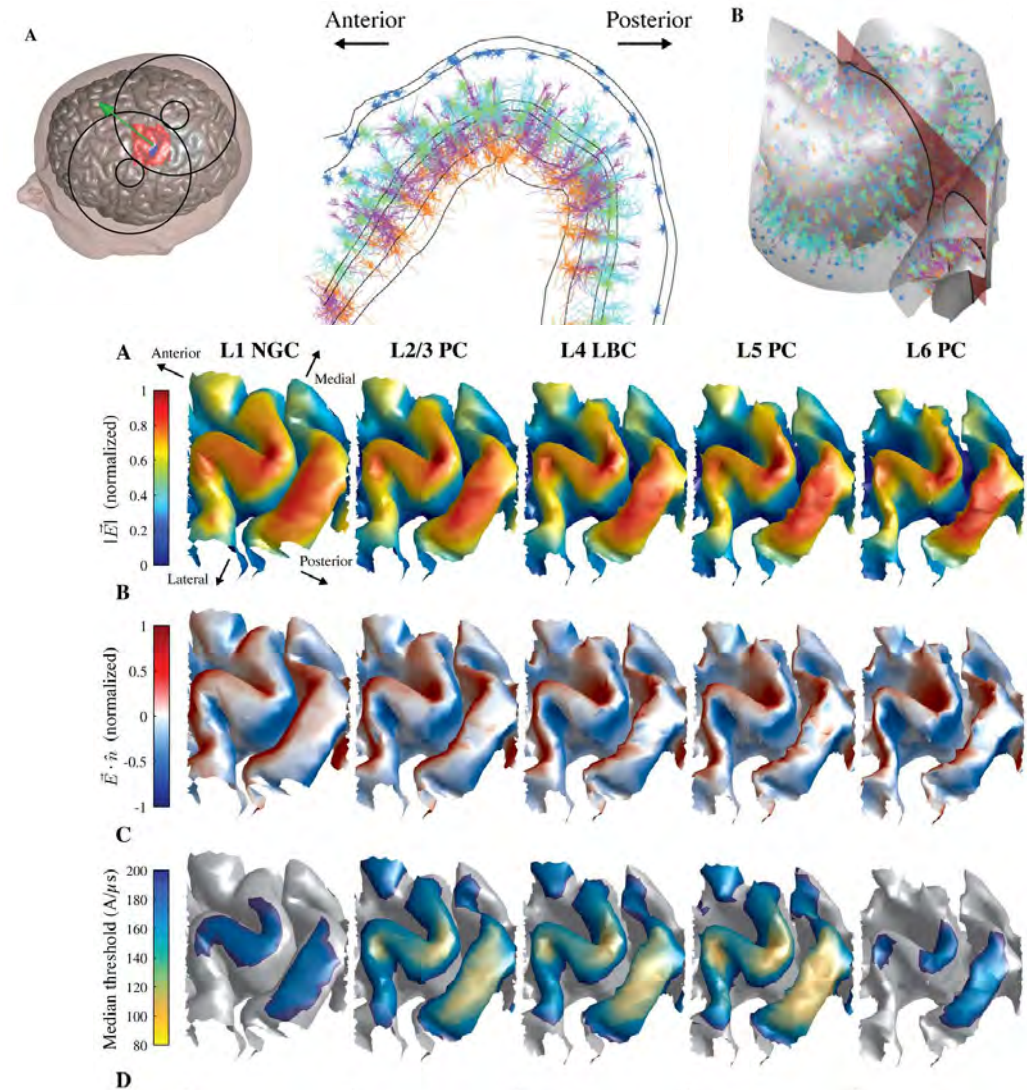


Note: Naming for \mathbf{J} follows the same convention: normJ vs J_{normal}

Interpretation of simulated electric fields: TMS

Mechanism-of-action

- TMS likely stimulates the **cortical sheet**
- Rough approximation: **Field strength** is the dominant factor determining neural excitation (Thielscher, NI, 2011; Bungert, Cer Cortex, 2016)
- This might be due to a preferential **activation of axon terminals** (Aberra et al., bioRxiv, 506204)
- Opposing hypothesis (Fox, HBM, 2004): **Normal component** of the electric field relative to the cortex is important



Interpretation of simulated electric fields: TES

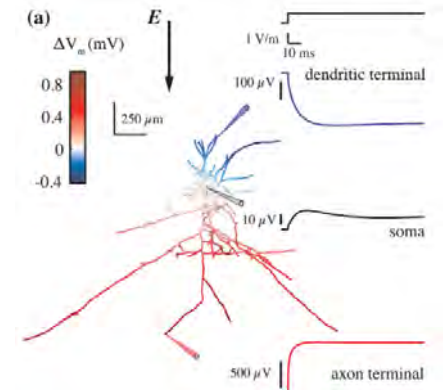
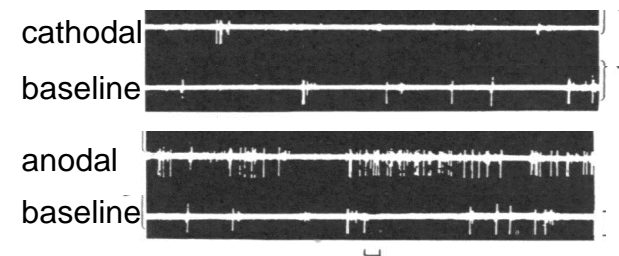
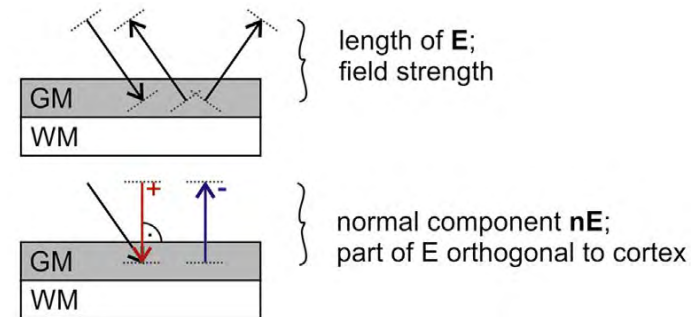
Normal component of the field is thought to be relevant for physiological effects

- Polarity-dependent stimulation effects on **cortical sheet**
- Fields **parallel** to the somato-dendritic axis polarize soma and dendrites of pyramidal cells: **Hyperpolarization near the anode and depolarization near the cathode**

This view is simplified

- Electric fields **perpendicular** to the apical–dendritic axis polarize **axon terminals**; occurs also for interneurons
- Seen, e.g. as modulation of responses to orthodromic stimulation

(Bindmann, *J Phys*, 1964; Bikson et al *J Physiol* 2004; Rahman *J Physiol*. 2017; Aberra et al *J. Neural Eng.* 2018)

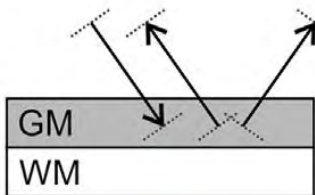


Electric field strength vs normal component

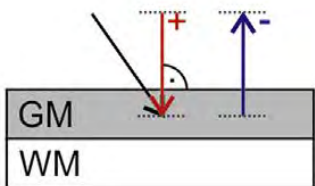
Example: Bipolar F3-F4 electrode montage

Observations:

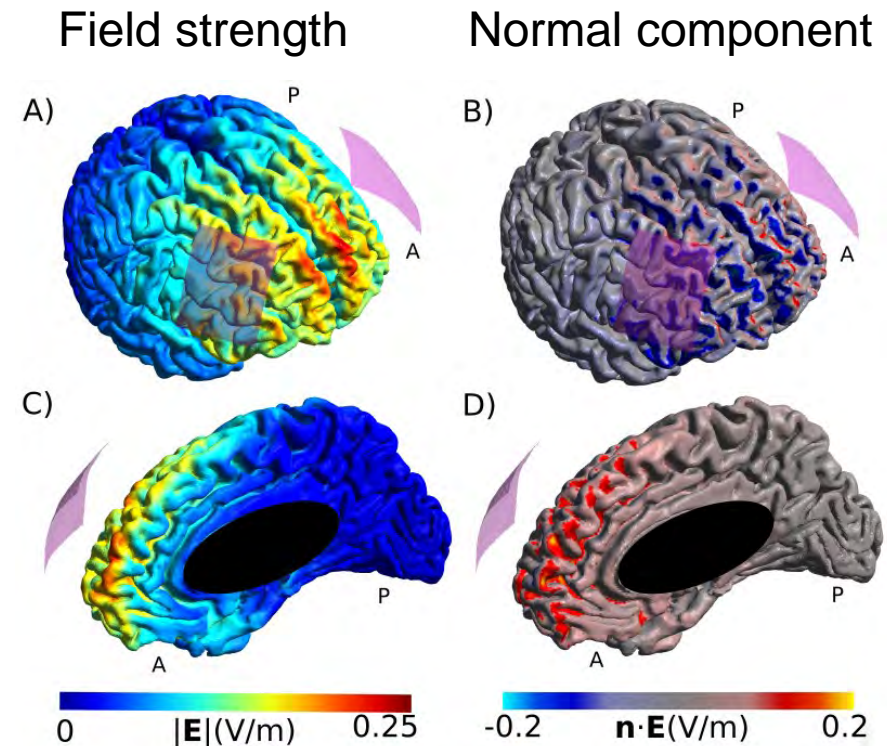
- **normE**: Highest field strengths close to the midline in the medial frontal cortex and not under the electrodes
- **E_normal**: Complex spatial stimulation pattern: Cathodal – anodal – cathodal – anodal



length of \mathbf{E} ;
field strength
vector norm of \mathbf{E}
→ **normE, or E_{norm}**



normal component $n\mathbf{E}$;
part of \mathbf{E} orthogonal to cortex
→ **E_{normal}**



(Karabanov, Front. Neuroscience, 2019)

From TDCS to TACS (and TRNS)

Quasi-static regime at low frequencies:

- **Electric field separates into spatial and temporal components.** The spatial component can be determined using Laplace's equation for the electrostatic field

$$\mathbf{E}(\mathbf{p}, t) = \mathbf{E}(\mathbf{p})I(t)$$

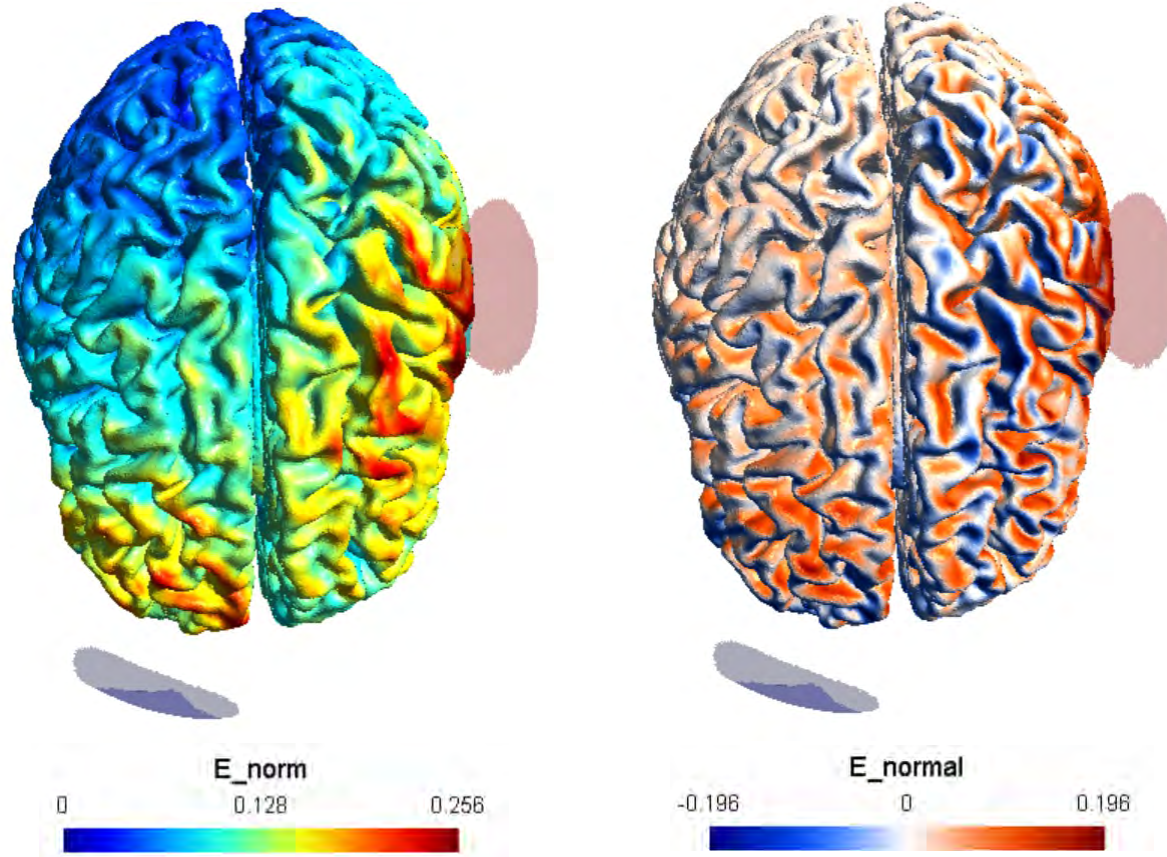
- Numerical field calculations (FEM) to get the spatial component.
- Multiplication of spatial component with temporal waveform gives electric field

- For > 2 electrodes, the field is the vector sum of the fields of the electrode pairs

$$\mathbf{E}(\mathbf{p}, t) = \sum_{i=1}^N \mathbf{E}_i(\mathbf{p}, t) = \sum_{i=1}^N \mathbf{E}_i(\mathbf{p}) I_i(t)$$

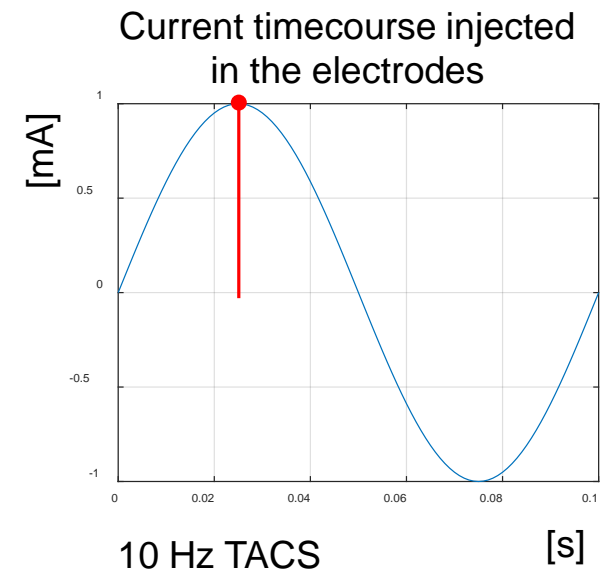
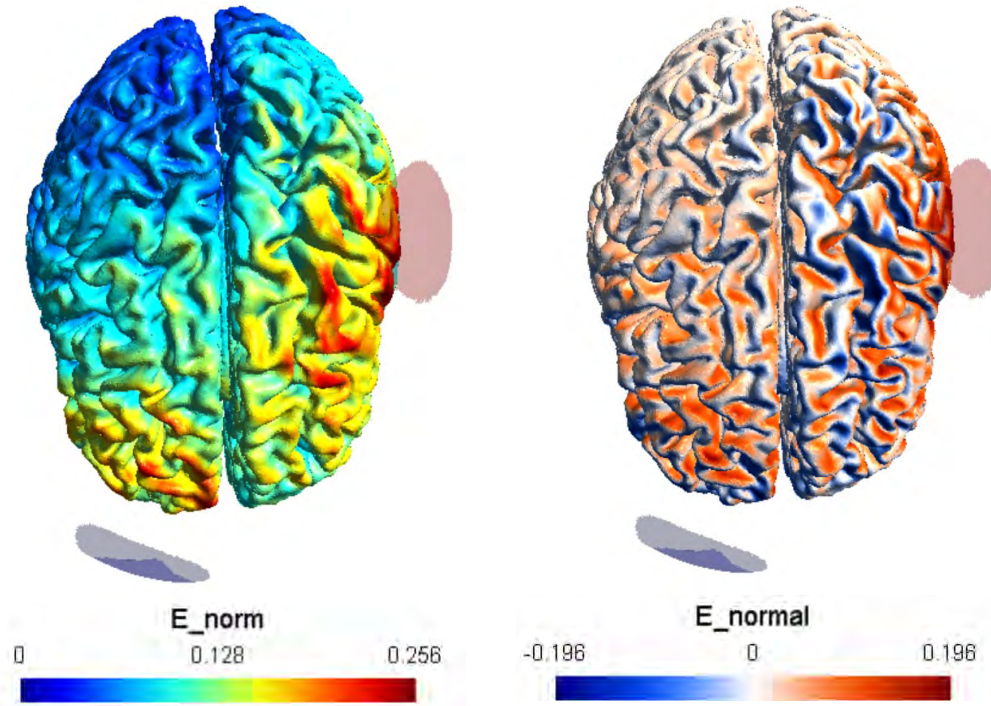
From TDCS to TACS (and TRNS)

Example: "Classical" M1 montage, 1 mA, anodal TDCS



From TDCS to TACS (and TRNS)

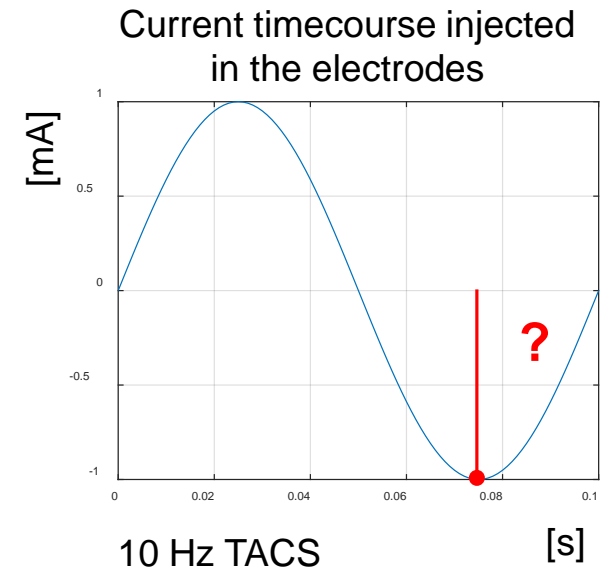
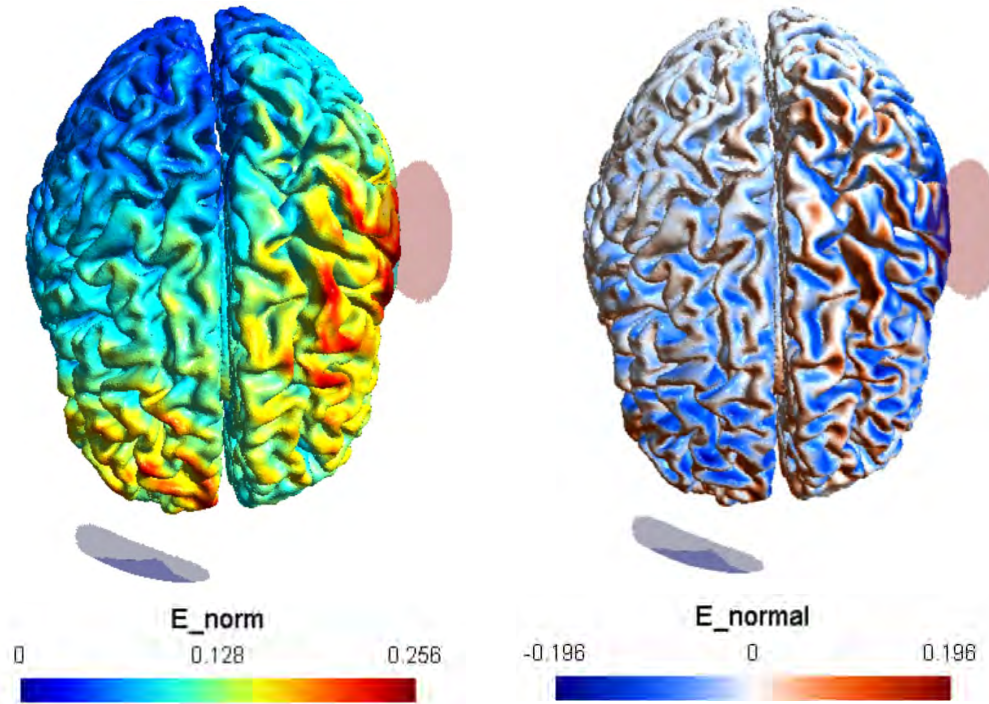
Example: "Classical" M1 montage, 1 mA, 10 Hz TACS



$$E(\mathbf{p}, t) = E(\mathbf{p}) \Big|_{1 \text{ mA}} \cdot \sin(2\pi ft)$$

From TDCS to TACS (and TRNS)

Example: “Classical” M1 montage, 1 mA, 10 Hz TACS



$$E(p, t) = E(p) \Big|_{1 \text{ mA}} \cdot \sin(2\pi ft)$$

- Repetitive change between hyper- and depolarization
- Regions with **same color** change polarity **in-phase**
- Regions with **opposite color** change polarity **anti-phase**

TRNS

Suggestion: Report the power of the noise signal

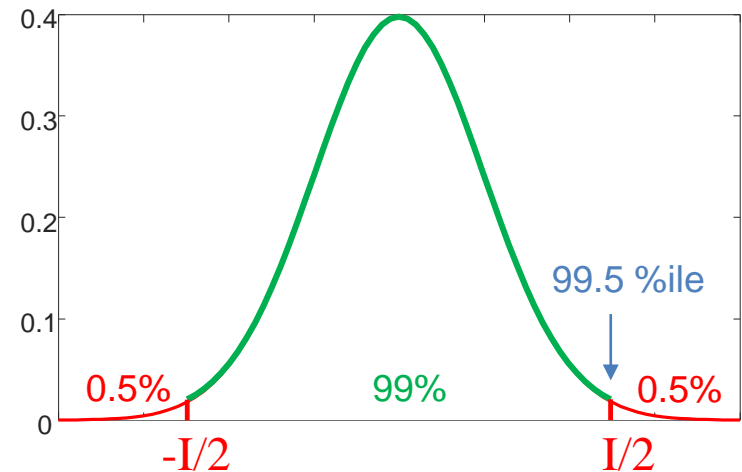
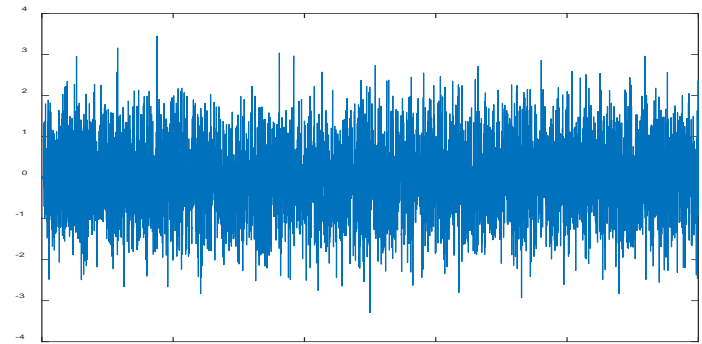
NeuroConn user manual: “noise” mode
“The random current levels are **statistically normally distributed** over time. ... The signal form noise has a bandwidth from 0 to 250 Hz.

...

Current I [μA]: 99% of the generated current levels are within the interval $[-\text{current}/2]$ and $[\text{current}/2]$.”

The **noise power** corresponds to the **variance ($=SD^2$)** of the Gaussian noise.

$$Z = \frac{X - \text{mean}}{SD} \quad SD = \frac{I/2}{Z(99.5\%ile)} \approx \frac{I}{5.15}$$



→ Simulate for $I/5.15$, and report this as the noise SD of the induced E-field